## CODE:1701-AG-F-4

## General Instructions :-

1. All question are compulsory.
2. The question paper consists of 26 questions divided into three sections $\mathrm{A}, \mathrm{B}$ and C. Section - A comprises of 6 question of 1 mark each. Section - B comprises of 13 questions of 4 marks each and Section - C comprises of 7 questions of 6 marks each .
3. There is no overall choice. However, internal choice has been provided in 4 question of four marks and 2 questions of six marks each. You have to attempt only one lf the alternatives in all such questions.
4. Use of calculator is not permitted.
5. Please check that this question paper contains 8 printed pages.
6. Code number given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.

## सामान्य निदे ${ }_{\mathrm{T}}$ :

1. सभी प्र न अनिवार्य हैं।
2. इस प्रश्न पत्र में 26 प्रश्न है, जो 3 खण्डों में अ, ब, व स है। खण्ड - अ में 6 प्रश्न हैं और प्रत्येक प्रश्न 1 अंक का है। खण्ड - ब में 13 प्रश्न हैं और प्रत्येक प्रश्न 4 अंको के हैं। खण्ड - स में 7 प्रश्न हैं और प्रत्येक प्रश्न 6 अंको का है।
3. प्रश्न संख्या 1 से 6 बहुविकल्पीय प्रश्न हैं। दिए गए चार विकल्पों में से एक सही विकल्प चुनें।
4. इसमें कोई भी सर्वोपरि विकल्प नहीं है, लेकिन आंतरिक विकल्प 4 प्रश्न 4 अंको में और 2 प्रश्न 6 अंको में दिए गए हैं। आप दिए गए विकल्पों में से एक विकल्प का चयन करें।
5. कैलकुलेटर का प्रयोग वर्जित हैं ।
6. कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृश्ठ 4 हैं।
7. प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए कोड नम्बर को छात्र उत्तर-पुस्तिका के मुख-पृश्ठ पर लिखें। Time: 3 Hours
Maximum Marks : 100
Total No. Of Pages :4

अधिकतम समय : 3
अधिकतम अंक : 100
कुल पृष्ठों की संख्या : 4

CLASS - XII
MATHEMATICS

## SECTION A

| Q. | Using derivative, find the approximate percentage increase in the area of a circle if its radius is <br> increased by $2 \%$. |
| :--- | :--- |
| Q. 2 | Write the direction ratio of the following line $: \mathrm{x}=-3, \frac{\mathrm{y}-4}{3}=\frac{2-\mathrm{z}}{1}$ |
| Q.3 | If A is a square matrix satisfying $A^{T} A=I$. Write the value of $\|A\|$. |
| Q.4 | Give an example of a skew symmetric matrix of order 3. |
| Q.5 | Find the derivative of $\left(\mathrm{e}^{\tan \mathrm{x}}\right)$ w.r. to x at $\mathrm{x}=0$. It is given that $\mathrm{f}^{\prime}(1)=5$. |

Visit us at www.agyatgupta.com

| Q. 6 | A plane meets the co - ordinates axes at $\mathrm{A}, \mathrm{B}$ and C respectively such that centroid of triangle ABC is $(1,-2,3)$. Find the equation of the plan. |
| :---: | :---: |
|  | SECTION B |
| Q. 7 | Without expanding the determinant at any stage, prove that $\left\|\begin{array}{ccc}\mid x+y & x & y \\ p y+z & y & z \\ 0 & p x+y & p y+z\end{array}\right\|=0$ if $x, y, z$ are in GP, where $x \neq y \neq z$ and $p$ is any real numbers. |
| Q. 8 | Find all point of discontinuity of f , where f is defined as following : $f(x)=\left\{\begin{array}{cc}\|x\|+3 & i f x \leq-3 \\ -2 x & -3<x<3 \\ 6 x+2 & i f x \geq 3\end{array}\right\}$. |
| Q. 9 | Find the vector equation of the line parallel to the line $\frac{x-1}{5}=\frac{3-y}{2}=\frac{z+1}{4}$ and passing through the point ( $3,0,-4$ ). Also find the distance between two lines . |
| Q. 10 | Evaluate : $\int \mathrm{e}^{2 \mathrm{x}} \cdot \sin (3 \mathrm{x}+1) \mathrm{dx}$. OR $\int \frac{x^{2}}{x^{4}+x^{2}+16} d x$ |
| Q. 11 | If $\mathrm{x}=\mathrm{a} \sin \mathrm{pt}, \mathrm{y}=\mathrm{b} \operatorname{cospt}$. Then find $\frac{\mathrm{d}^{2} \mathrm{y}}{\mathrm{dx}^{2}}$ at $\mathrm{t}=0$. |
| Q. 12 | Solve for $\mathrm{x}: \sin ^{-1}(1-x)-2 \sin ^{-1} x=\frac{\pi}{2}$ |
| Q. 13 | Find the mean, the variance and the standard derivation of the number of doublets in three throws of a pair of dice. |
| Q. 14 | Find the interval in which the function $f(x)=(x+1)^{3}(x-3)^{3}$ is strictly increasing or strictly decreasing. Also, find the points of local maximum and local minimum, if any. |
| Q. 15 | Form the differential equation representing the family of ellipse having foci on x -axis and centre at the origin. <br> OR <br> Form the differential equation of the family of circles having radii 3 . |
| Q. 16 | Find : $\int_{0}^{\pi / 4} \frac{d x}{\cos ^{3} x \sqrt{2 \sin 2 x}}$. <br> OR <br> Evaluate : $\int_{0}^{\pi / 4} \frac{\sec x}{1+2 \sin ^{2} x} d x$ |
| Q. 17 | Let $\mathrm{A}=\mathrm{Q} \times \mathrm{Q}$, where Q is the set of all rational numbers, and * be a binary operation on a defined by $(\mathrm{a}, \mathrm{b}) *(\mathrm{c}, \mathrm{d})=(\mathrm{ac}, \mathrm{b}+\mathrm{ad})$ for $(\mathrm{a}, \mathrm{b}),(\mathrm{c}, \mathrm{d}) \in \mathrm{A}$. Then find <br> (i) The identity element of * in A. <br> (ii) Invertible elements of A, <br> OR <br> Show that the relation $R$ in the set $N x N$ defined by (a, b) $R(c, d)$ iff $a^{2}+d^{2}=b^{2}+c^{2} \forall a, b, c, d \in N$, is an equivalence relation. |
| Q. 18 | Find the coordinates of the point where the line through the points $\mathrm{A}(3,4,1)$ and $\mathrm{B}(5,1,6)$ crosses the plane determined by the points $\mathrm{P}(2,1,2), \mathrm{Q}(3,1,0)$ and $\mathrm{R}(4,-2,1)$. |
| Q. 19 | Three schools A, B and C organized a mela for collecting funds for helping the rehabilitation of flood victims. They sold hand made fans, mats and plates from recycled material at a cost of Rs. |
| TMCID Ph. 23 PREM | 2 <br> Resi.: D-79 Vasant Vihar ; Office : 89-Laxmi bai colony 615; 4010685®, 2630601(O) Mobile : 9425109601 (P); $\underline{9907757815 ; ~} 9425110860 ; 425772164 ;$ Email:agyat99@ gmail.com. R INSTITUTE for $\mathrm{X}, \mathrm{XI} \& \mathrm{XII}$.© publication of any part of this paper is strictly prohibited. |

Visit us at www.agyatgupta.com

|  | 25, Rs. 100 and Rs. 50 each. The number of articles sold are given below |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | A | B | C |  |
|  | Hand- fa | 40 | 25 |  |  |
|  | Ma | 50 | 40 | 50 |  |
|  | Plate | 20 | 30 | 40 |  |
|  | Find the funds collected by each school separately by selling the above articles. Also find the total funds collected for the purpose. <br> Write one value generated by the above situation. |  |  |  |  |
|  | ECTION C |  |  |  |  |
| Q. 20 | If $A=\left[\begin{array}{ccc}1 & -1 & 0 \\ 2 & 5 & 3 \\ 0 & 2 & 1\end{array}\right]$, find $A^{-1}$ using elementary row transformation. |  |  |  |  |
| Q. 21 | An urn contains 3 red 5 black balls. A ball is drawn at random, its colour is noted and returned to the urn. Moreover, 2 additional balls of the colour noted down, are put in the urn and then two balls are drawn at random (without replacement) from the urn. Find the probability that both the balls drawn are of red colour. <br> OR <br> In an examination, 10 questions of true- false type are asked. A student tosses a fair coin and determine his answer to each question. If the coin falls heads, he answers true and if it falls tails, he answers false. Show that the probability that he answers at most 7 questions correctly is $\frac{121}{128}$. |  |  |  |  |
| Q. 2 | Using integration find the area of the region bounded by the parabola $x^{2}+y^{2}=32, \mathrm{x}$ axis and the line $x=y$ in the first quadrant. |  |  |  |  |
| Q. | Kellogg is a new cereal formed of a mixture of bran and rice that contains at least 88 grams of protein and at least 36 milligrams of iron. Knowing that bran contains 80 grams of protein and 40 milligrams of iron per kilogram, and that rice contains 100 grams of protein and 30 milligrams of iron per kilogram, find theminimum cost of producing this new cereal if bran costs Rs. 5 per kilogram and rice costs Rs. 4 per kilogram. |  |  |  |  |
| Q. 24 | If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} \cdot \vec{b}=\vec{a} \cdot \vec{c}=0$ and the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{6}$, then prove that (i) $\vec{a}= \pm 2(\vec{b} \times \vec{c})$, (ii) $[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}]= \pm 1$. |  |  |  |  |
| Q. | Find the area of the region enclosed by the parabola $x^{2}=y$ the line $\mathrm{y}=\mathrm{x}+2$ and the x - axis . |  |  |  |  |
| Q. 26 | A wet porous substance in the open air loses its moisture at a rate proportional to the moisture content .If a sheet hung in the wind loses half its moisture during the first hour, when will it have lost $90 \%$, weather conditions remaining the same? <br> OR <br> Solve the following differential equation, given that $y=0$, when $x=\frac{\pi}{4}: \sin 2 x \frac{d y}{d x}-y=\tan x$. |  |  |  |  |
|  | A MAN WHO DOESN'T TRUST HIMSELF ; CAN NEVER TRULY TRUST ANYONE ELSE |  |  |  |  |

Visit us at www.agyatgupta.com
42 SELECTIONS IN JEE ADVANCED, 2015


Rishabh Singh AIR - 434


Aditya Sharma AIR - 666


Ankur Yadav AIR - 700


Shiv Kumar AIR - 1001


Deepesh Nathani AIR - 1525


Abhay Raghav AIR - 1931


Utkarsh Mishra AIR - 2574


Nishtha Saxena AIR - 6209


Arun Suri
AIR - 8016


Gargi Gupta
AIR - 3573


Satyam Mishra AIR - 6259


Siddhant Jain AIR - 8118


Sandeep Prajapati
AIR - 3689


Mritunjay Bhadoria
AIR - 5356


Ashish Anand
AIR - 5470
 AIR - 6966


Utkarsh Sharma


Aviral Singhal AIR - 7021


Kartikeya Agarwal
AIR - 12952


$\begin{array}{cc}\text { Rahul Ashna } & \\ \text { AIR - } 16814 & \text { AIR } \\ & \end{array}$


Aman Jha


Sakshi Parashar
AIR - 18368


Mohit Sharma


An institute for JEE (Main+Advanced) / Medical Gorious Performance
by Pinnacle Student's in JEE Advanced 2015

## 36, Laxmibai Colony, Padav, Gwalior Ph. 0751-4014124, 2444124, 4012615

